

**B.Sc. 2<sup>nd</sup> Semester (Honours) Examination, 2020-21****PHYSICS****Course ID: 22411****Course Code: SH/PHS/201/C-3**

Course Title: Electricity and Magnetism

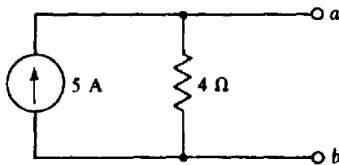
**Time: 1 Hour 15 Minutes****Full Marks: 25**

*The figures in the margin indicate full marks.  
Candidates are required to give their answers in their own words  
As far as practicable*

**Section-I**1. Answer any *five* questions.

1 × 5 = 5

- (a) A regular tetrahedron consisting of a charge of +Q C at its centroid. Find the flux of electric field through any one of its face.
- (b) State the Gauss's law in magnetostatics mentioning its significance.
- (c) Show that the potential distribution within a conducting medium satisfies Laplace's equation as long as the medium is homogeneous and the current distribution is time invariant or steady.
- (d) What do you mean by conservative field?
- (e) Define electric susceptibility.
- (f) What is the significance of the area of a B-H loop?
- (g) When an ordinary 'current source' can be renamed as 'constant current source'?
- (h) Transform the following current source into a voltage source.

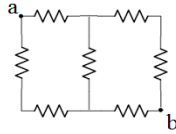
**Section-II**2. Answer any *two* questions:

5 × 2 = 10

- (a) (i) Using Gauss's law, find electric field inside a parallel plate air filled capacitor (taking +σ and -σ as the existing surface charge densities on the two plates respectively).
- (ii) Write down the differential form of Gauss's law. Suppose that electric field in some region is found to be  $\vec{E} = \alpha r^3 \hat{r}$  V/m in spherical coordinates ( $\alpha$  is a constant). Find the electric charge density in the region. [2+(1+2)]
- (b) (i) Write down the defining equation of fundamental magnetic field and mention the significance.
- (ii) From Biot-Savart's law show that  $\vec{\nabla} \cdot \vec{B} = 0$ . P.T.O

(iii) Find energy magnetic field at the centre of a regular hexagonal loop of side  $a$  carrying current  $I$ . [1+2+2]

(c) (i) Find the equivalent resistance between point  $a$  and  $b$  for the following resistance configuration where resistance of each resistor is 10 ohm.



(ii) Find the vector electric field at  $(1,1,1)$  due to the charges  $+1C(1,0,0)$ ,  $+1C(0,1,0)$  and  $+1C(0,0,1)$  [3+2]

(d) (i) Find capacitance of a Spherical capacitor of shell radii  $a$  and  $b$  respectively ( $a < b$ ). Hence find the capacitance of an isolated sphere.

(ii) Show that  $\vec{\nabla} \times \vec{E} = -\partial \vec{B} / \partial t$  in time varying era and mentioning the laws associated with it. [3+2]

### Section-III

3. Answer any **one** question: 10 × 1 = 10

(a) (i) Find  $\vec{B}$  at a point on the axis of an infinitely long air-core solenoid carrying current  $I$  with no. of turns per unit length being  $n$ . What will be the magnetic field at the end of such solenoid?

(ii) Show that the electric field due to an electric dipole at a far away field point can be expressed as:

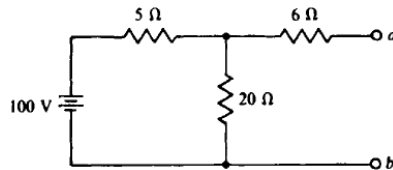
$$\vec{E} = \frac{1}{4\pi\epsilon} \left[ \frac{3(\vec{p} \cdot \vec{r})\vec{r}}{r^5} - \frac{\vec{p}}{r^3} \right]; \text{ where symbols have their usual meanings. } \quad [(4+1)+5]$$

(b) (i) Prove that dielectric displacement vector  $\vec{D}$  can be related to total Electric field ( $\vec{E}$ ) and Polarization vector as:  $\vec{D} = \epsilon_0 \vec{E} + \vec{P}$ . Hence show that  $\epsilon_r = 1 + \chi_e$ . (symbols have their usual meanings)

(ii) The permittivity of the dielectric material between the plates of a parallel-plate capacitor (inter-plate separation  $d$  and plate area  $A$ ) varies uniformly from  $\epsilon_1$  to  $\epsilon_2$  from one plate to another. Show that the capacitance of the capacitor ( $C$ ) can be expressed as:

$$C = \frac{A}{d} \ln(\epsilon_2 / \epsilon_1)$$

(iii) Find the resistance of the resistor which draws a current of 5A when connected across  $a$  and  $b$  of the circuit below.



[(3+1)+3+3]